

〈解答〉

- ① (1) $20xy - 15y^2$ (2) $6x - 7$ (3) $xy + 5x + 2y + 10$
 (4) $2x^2 - 7x - 15$ (5) $a^3 - b^3$ (6) $x^3 - x^2 - 22x - 48$
 (7) $x^2 + x - 20$ (8) $x^2 + 6x + 9$ (9) $x^2 - 16x + 64$
 (10) $x^2 - 49$ (11) $-x^2 - 11x + 16$ (12) $-10a + 89$
 (13) $2x^2 + 10x + 4$ (14) $a^2 + 2ab + b^2 + 3a + 3b - 40$
 (15) $x^2 + 2xy + y^2 - 4x - 4y + 4$
- ② (1) $2x(2y - z)$ (2) $-3pr(3q - 7)$ (3) $(x + 8)(x + 12)$
 (4) $(b - 3)(b - 5)$ (5) $(x + 6)^2$ (6) $(a - 7)^2$
 (7) $(a + 9)(a - 9)$ (8) $2(x + 2)(x + 6)$ (9) $3b(a + 5c)(a - 5c)$
 (10) $(a - 2)(x - 2)$ (11) $(x - 6)(x - 4)$ (12) $(a - b)(a + 3)$
- ③ (1) -14 (2) -36 (3) 41 (4) 9 (5) 22

配点 ①, ②は各1点, ③は各2点 37点満点

〈解説〉

- ① (11) $(x - 4)^2 - x(2x + 3)$ (12) $(a - 5)^2 - (a + 8)(a - 8)$
 $= x^2 - 8x + 16 - 2x^2 - 3x$ $= a^2 - 10a + 25 - (a^2 - 64)$
 $= -x^2 - 11x + 16$ $= a^2 - 10a + 25 - a^2 + 64$
 $= -10a + 89$
- (13) $(x + 3)^2 + (x + 5)(x - 1)$ (14) $(a + b - 5)(a + b + 8)$
 $= x^2 + 6x + 9 + x^2 + 4x - 5$ $a + b = M$ とおくと,
 $= 2x^2 + 10x + 4$ $= (M - 5)(M + 8)$
 $= M^2 + 3M - 40$
 もとにもどすと,
 $= (a + b)^2 + 3(a + b) - 40$
 $= a^2 + 2ab + b^2 + 3a + 3b - 40$
- (15) $(x + y - 2)^2$
 $x + y = M$ とおくと,
 $= (M - 2)^2$
 $= M^2 - 4M + 4$
 もとにもどすと,
 $= (x + y)^2 - 4(x + y) + 4$
 $= x^2 + 2xy + y^2 - 4x - 4y + 4$
- ② (8) $2x^2 + 16x + 24$ (9) $3a^2b - 75bc^2$
 $= 2(x^2 + 8x + 12)$ $= 3b(a^2 - 25c^2)$
 $= 2(x + 2)(x + 6)$ $= 3b(a + 5c)(a - 5c)$

$$\begin{aligned}
 (10) \quad & ax - 2x - 2a + 4 \\
 &= x(a-2) - 2(a-2) \\
 &\quad a-2 = M \text{とおくと,} \\
 &= xM - 2M \\
 &= M(x-2) \\
 &\quad \text{もとにもどすと,} \\
 &= (a-2)(x-2)
 \end{aligned}$$

$$\begin{aligned}
 (11) \quad & (x-3)^2 - 4(x-3) + 3 \\
 &\quad x-3 = M \text{とおくと,} \\
 &= M^2 - 4M + 3 \\
 &= (M-3)(M-1) \\
 &\quad \text{もとにもどすと,} \\
 &= \{(x-3)-3\} \{(x-3)-1\} \\
 &= (x-6)(x-4)
 \end{aligned}$$

$$\begin{aligned}
 (12) \quad & a^2 - ab + 3a - 3b \\
 &= a(a-b) + 3(a-b) \\
 &\quad a-b = M \text{とおくと,} \\
 &= aM + 3M \\
 &= M(a+3) \\
 &\quad \text{もとにもどすと} \\
 &= (a-b)(a+3)
 \end{aligned}$$

$$\begin{aligned}
 \text{③ (1)} \quad & (-4a^2b + ab^2 - 2ab) \div (-ab) \\
 &= 4a - b + 2
 \end{aligned}$$

これに, $a = -3$, $b = 4$ を代入すると,
 $4 \times (-3) - 4 + 2 = -14$

$$\begin{aligned}
 (2) \quad & (x-2y)(x+8y) - (x+4y)(x-4y) \\
 &= x^2 + 6xy - 16y^2 - (x^2 - 16y^2) \\
 &= x^2 + 6xy - 16y^2 - x^2 + 16y^2 \\
 &= 6xy
 \end{aligned}$$

これに, $x = 3$, $y = -2$ を代入すると,
 $6 \times 3 \times (-2) = -36$

$$\begin{aligned}
 (3) \quad & (a-b)(a+2b) - ab \\
 &= a^2 + ab - 2b^2 - ab \\
 &= a^2 - 2b^2
 \end{aligned}$$

これに $a = 7$, $b = -2$ を代入すると,
 $7^2 - 2 \times (-2)^2 = 49 - 8 = 41$

$$\begin{aligned}
 (4) \quad & x^2 - y^2 \\
 &= (x+y)(x-y) \\
 &\quad \text{これに, } x=3.75, y=2.25 \text{ を代入すると,} \\
 &\quad (3.75+2.25) \times (3.75-2.25) = 6 \times 1.5 = 9
 \end{aligned}$$

$$\begin{aligned}
 (5) \quad & x^2 + xy + y^2 \\
 &= x^2 + 2xy + y^2 - xy \\
 &= (x+y)^2 - xy \\
 &\quad \text{これに, } x+y = -5, xy = 3 \text{ を代入すると,} \\
 &\quad (-5)^2 - 3 = 25 - 3 = 22
 \end{aligned}$$